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# High-*T*<sub>c</sub> Cooper-pair injection in a semiconductor–superconductor structure

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to low critical temperature of the superconductor being used

ing a high critical temperature (above the boiling temper-

ature of liquid nitrogen of 77 K). Realization of high- $T_{\rm c}$ 

superconductor-semiconductor light-emitting structures can

allow using quantum optics to probe high- $T_c$  superconductors. Although there has been an unprecedented effort to under-

stand the mechanism of high- $T_c$  superconductivity, it still remains unsolved. This difficulty stems largely from the fact

that even in the normal state above  $T_c$ , these materials are

not well-understood. Superconductivity is obtained by impu-

rity doping, and the parent material is an antiferromagnetic strongly-correlated Mott insulator [15], where single-particle

band theory description fails. Recent studies have revealed a

complex phase diagram vs temperature and doping, as well as the unconventional d-wave symmetry of the order parameter in high- $T_c$  materials [16, 17]. Other aspects are still being debated—such as the appearance of self-organization with non-uniform charge carrier density (stripes) [18], and the ori-

gin of the pseudogap phase [19, 20] with possible relation

High- $T_{\rm c}$  superconductors have the strong advantage of hav-

#### Abstract

We observe Andreev reflection in a YBCO–GaN junction through differential conductance spectroscopy. A strong characteristic zero-bias peak was observed and persisted up to the critical temperature of the superconductor with a smaller superconducting order parameter  $\Delta \sim 1 \text{ meV}$ . The presence of Andreev reflection with the small  $\Delta$  in comparison to its value for high- $T_c$  superconductors forms an important milestone toward demonstration of superconducting proximity in high- $T_c$ /semiconductor junctions. Experimental results were then compared to the theoretical model with good agreement. Efficient injection of Cooper pairs into direct bandgap semiconducting structures, together with high transition temperature of YBCO, can pave the way to novel optoelectronics and quantum optical studies of high- $T_c$ materials.

Keywords: high-T<sub>c</sub> superconductivity, superconductor-semiconductor, Andreev reflection

(Some figures may appear in colour only in the online journal)

Hybrid superconductor-semiconductor structures form a rapidly growing field of research [1, 2], which utilizes the unique physical properties of the superconducting state [3] along with the vast knowledge and fabrication capabilities in the field of semiconductors. Various applications involving such hybrid structures have been shown, including superconducting light-emitting diodes (SLEDs) and quantum dots [4–6], Bell-state analyzers [7] and superconductor-based waveguide amplifiers [8]. Of note is the SLED which is a hybrid superconductor-semiconductor device, where superconducting Cooper pairs recombine with semiconductor hole pairs, forming polarization-entangled photon pairs [9]. While low- $T_{\rm c}$  Cooper-pair injection into semiconductors has been observed previously [10-13], including the recent demonstration of radiative recombination of Cooper pairs in SLED devices [14], they must operate at very low temperatures due

 $(\sim 10 \text{ K}).$ 

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to the formation of Cooper pairs without condensation above  $T_c$ . Various experimental techniques have been employed to study unconventional superconductivity—ranging from electrical transport and tunneling [21–28] to infrared electrodynamics [16], resulting in a substantial body of knowledge. However, these techniques do not have access to the phase information of individual charge carriers, or various correlations within the Cooper pairs such as classical spin and momentum correlations, as well as quantum entanglement. Optical access to individual charge carriers through quantum light–matter interaction with relative phase information and quantum correlations can provide important insights into the nature of unconventional superconductivity and pave the way for novel optoelectronics.

The challenge in using high- $T_c$  superconductors is that their growth and fabrication poses a greater challenge in comparison to their low- $T_c$  counterparts [29]. High- $T_c$  superconductors require stringent growth conditions and can degrade rapidly when incorporated into a given semiconductor device or even under standard ambient conditions [30, 31]. Nevertheless, devices incorporating high- $T_c$  superconductors have been successfully demonstrated. These include terahertz sources [32], RF SQUIDs [33] and YBCO–Graphene junctions [34] to name a few. In addition, much research has been done on Andreev bound states in high- $T_c$  superconductors [24–28].

The second required component for the high- $T_c$  superconductor–semiconductor junction is a semiconductor such as GaN which has a decomposition temperature of 1300 K [35], a property enabling it to serve as the growth substrate for YBCO at high temperatures [36, 37]. Epitaxial growth of YBCO on GaN was demonstrated recently, however no Cooper pair injection was achieved [38].

Here we demonstrate high- $T_c$  Cooper-pair injection in a superconductor–semiconductor junction (YBCO–GaN), exhibiting strong Andreev reflection in the electrical conductance spectra. High injection efficiency was achieved by improving the semiconductor–superconductor interface and optimizing the YBCO growth process. The combination of YBCO with a GaN-based LED structure allows for the design of high-temperature SLEDs. A model for describing the electrical conductance of high- $T_c$  superconductor–semiconductor junctions [39] was then used in good agreement with our experimental observations.

For our experiments, a 3.5  $\mu$ m thick *n*-GaN layer ( $n \sim 5 \times 10^{18} \text{ cm}^{-3}$ ) with the top 200 nm thick heavily doped ( $\sim 2 \times 10^{19} \text{ cm}^{-3}$ ) was initially grown on buffered Al<sub>2</sub>O<sub>3</sub> substrate. A 100 nm YBCO layer was then grown in a suitable high vacuum chamber using a customized pulsed laser deposition system [40]. A KrF excimer laser (248 nm) with pulse energy of 38 mJ and a repetition rate of 2 Hz was used. The sample was heated up to a temperature of 650 °C at a rate of 18 °C min<sup>-1</sup> and was kept under oxygen pressure of 0.195 mbar for the duration of the growth. After growth was completed, that sample was cooled down at a rate of 18 °C min<sup>-1</sup> in a 100 mbar oxygen atmosphere to avoid the formation of oxygen vacancies.

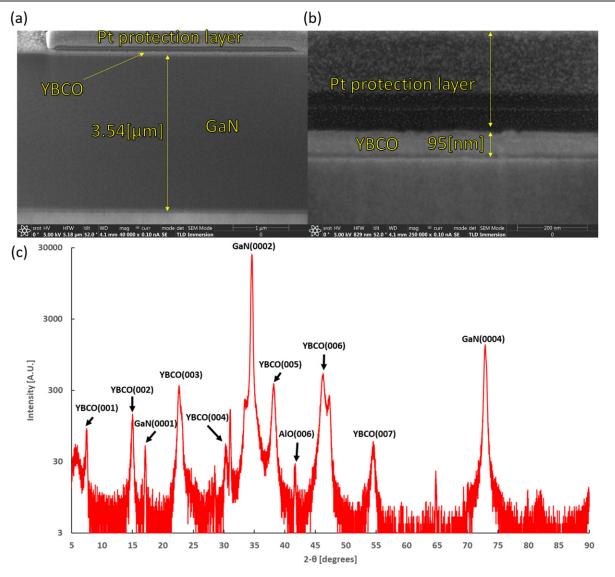
For characterization an XRD test was performed (figure 1(c)) to check for the composition of the various layers. The obtained XRD profile matched the XRD profile

from the previous work with the same characteristic peaks indicating a layer stack composed of YBCO, GaN and a Sapphire substrate. Additional characterization was performed using SEM (figures 1(a) and (b)) where a portion of the sample was etched using a focused ion beam. The test revealed a top YBCO layer with 100 nm thickness. Below the YBCO layer was a 3.5  $\mu$ m GaN layer followed by the sapphire substrate.

Following the growth of multiple samples, half of each sample was dipped in a solution of 0.01% H<sub>3</sub>PO<sub>4</sub> in order to remove the top YBCO layer and expose the bottom GaN layer. The samples were then placed inside a ceramic chip holder (LCC28) with aluminum wires being bonded to both YBCO and GaN layers via wedge bonding. The samples were then inserted into the cryostat for testing.

The measurement of temperature dependent resistance has revealed a critical temperature of about  $\sim 80$  K which is close to the maximum reported value of 93 K for YBCO [41]. Residual series resistance of  $\sim 120 \ \Omega$  below  $T_c$  was also observed and is attributed to non-superconducting regions of the device. The wide transition between the normal and superconducting state (figure 2(b)) can be attributed to multiple domains inside the superconductor having different critical temperatures. Thus, true global superconductivity is obtained at a lower (albeit still high) temperature (~80 K) in comparison to an ordered superconductor. Since YBCO/GaN growth was first demonstrated very recently [38] the growth process may not be fully optimized; however, important information can be extracted from our measurements. Both the broadening and reduced T<sub>c</sub> can be attributed to large defect density and diffusion of Ga atoms from the GaN layers into the YBCO [38]. As the exact profile of the diffused Ga atoms is unknown, we cannot pinpoint the exact location inside the junction where Andreev reflection takes place. Electrical transport measurements were then conducted using four-probe configuration (figure 2(a)). This configuration ensures that only the sample resistance is measured and not the wires or the sample-wire interface. This is due to the fact that the only measured voltage is the voltage drop on the device itself. Thus even if Andreev reflection does take place between the YBCO and the aluminum bonding wires, it will not appear in our measurement. The conductance measurements (figure 3) revealed a strong zero-bias peak with significant dependence on the temperature of the junction. The peak conductance decreases as the temperature increases up to the critical temperature. The width of the zero-bias peak increases with increasing temperature due to the growing thermal energy of the charge carriers, which broadens the peak.

In order to model the experimental results we used a theoretical description of carrier injection and the resulting conductance spectra of high- $T_c$  superconductor–semiconductor junctions formulated by Tanaka and Kashiwaya [39]. The model is based on the Blonder–Tinkham–Klapwijk (BTK) theory [42] describing the behavior of quasiparticle excitations from the superconducting state. Using the quasiparticle description, the electrical conductance spectra can be calculated. The complete wave function is composed of two



**Figure 1.** (a) and (b) SEM images of the entire device stack showing a 3.5  $\mu$ m GaN layer with a thin YBCO layer on top. The Pt protection layer was added during SEM imaging. (c) XRD peak spectrum of the measured sample. Characteristic peaks to YBCO, GaN and sapphire (AlO) were measured.

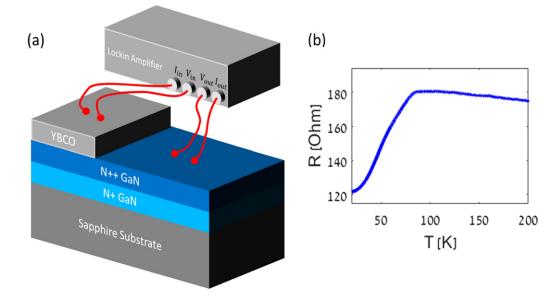
components, satisfying the Bogoliubov-de-Gennes equations:

$$\begin{cases} \left[ -\frac{\hbar^2}{2m} \frac{\mathrm{d}^2}{\mathrm{d}x^2} - \mu(x) + V(x) \right] \cdot u(x) + \Delta(x) \cdot v(x) = E \cdot u(x) \\ - \left[ -\frac{\hbar^2}{2m} \frac{\mathrm{d}^2}{\mathrm{d}x^2} - \mu(x) + V(x) \right] \cdot v(x) + \Delta(x) \cdot u(x) = E \cdot v(x) \end{cases}$$
(1)

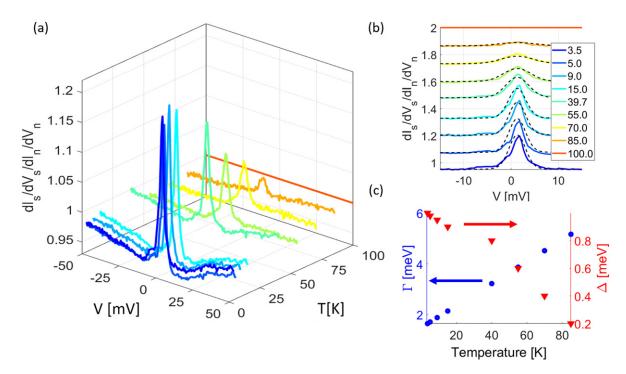
With  $\mu(x)$ , V(x),  $\Delta(x)$  being the chemical potential, potential barrier and the superconducting order parameter correspondingly, and u(x), v(x) being the quasiparticle wave functions. A delta barrier is assumed to exist at the superconductor-semiconductor interface having an effective barrier strength parameter  $Z = H/\hbar v_f$  where  $v_f$  is the Fermi velocity and *H* is the height of the delta barrier. For a small *Z*, the junction is transparent and Andreev reflection takes place, while for a large *Z* Andreev reflection is inhibited and the tunneling regime takes place. While the original BTK model copes with superconductors described by the BCS model, YBCO is a not a BCS superconductor and thus the anisotropic model [39] is required. This model takes into account the *k* dependence of the superconducting order parameter  $\Delta$ . If an s-wave superconductor is assumed, equations of the model reduce to the original BTK model equations. Since we included a broadening term in our model, the results for either d-wave or s-wave models result in similar spectra. The normal junction conductivity is expressed as  $\sigma_N \triangleq \frac{4\lambda}{(1+\lambda)^2+4Z^2}$  where  $\lambda$  is the wave-vector mismatch between the superconductor and semiconductor. The resulting normalized conductance is:

$$\sigma_{\rm R} = \frac{1 + \sigma_{\rm N} |\Gamma_{+}|^{2} + (\sigma_{\rm N} - 1) |\Gamma_{+} \Gamma_{-}|^{2}}{\left|1 + (\sigma_{\rm N} - 1) \Gamma_{+} \Gamma_{-} \exp(i[\varphi_{-} - \varphi_{+}])\right|^{2}}, \quad (2)$$

where  $\Gamma_{\pm} = \frac{E - \Omega_{\pm}}{|\Delta_{\pm}|}, \Omega_{\pm} = \sqrt{E^2 - |\Delta_{\pm}|^2}$  and  $\Delta_{\pm}$  is the pair



**Figure 2.** (a) Schematics of the device and four-probe measuring technique. (b) Measured sample resistance as function of temperature also done in a four-probe configuration (all four probes connected to the YBCO layer). Residual series resistance of non-superconducting YBCO was also observed.



**Figure 3.** (a) Normalized conductance spectra of the YBCO–GaN junction. A strong zero-bias peak is evident, decreasing in magnitude and broadening up to the critical temperature. (b) Measured (solid lines) and modeled (dashed lines) spectral shapes of the zero-bias peak. (c) Extracted dependence on the temperature of the order parameter  $\Delta(T)$  and broadening  $\Gamma(T)$ .

potential of the electron-like and hole-like quasiparticles and  $\varphi_+$  is the phase of each pair potential.

Using this model, a good agreement with theory was obtained (figure 3(b)) with an effective barrier strength Z of  $\sim 0.4$  and an induced superconducting order parameter  $\Delta$  of  $\sim 1$  meV. The small value obtained for the order parameter may be attributed to the proximity effect, as superconductivity is induced in the semiconductor albeit with a reduced magnitude of the order parameter  $\Delta$  (in relation to its value

in the parent superconductor) [43]. Earlier works [13] have also demonstrated similar behavior in Nb/Si junctions, with a reduced value of  $\Delta$ . Moreover, disorder in the superconductor can also lead to a reduction in the value of  $\Delta$  [44]. Such disorder can also be the cause behind the broadened transition in the resistance-temperature dependence (figure 2(b)). We have performed a fit for the superconducting gap  $\Delta$  as well as the broadening term  $\Gamma$ . We have used the general form  $\Gamma = \Gamma_0 + \alpha k_{\rm B}T$  where  $\Gamma_0$ ,  $\alpha$  are fitting coefficients,  $k_{\rm B}$  is the Boltzmann coefficient and T is the sample temperature. The obtained coefficients were  $\Gamma_0 = 1.5 \text{ [meV]}, \alpha = 1/2$ . For  $\Delta$ , a general fitting was performed with  $(T = 3.5 \text{ K}) \approx 1 \text{ [meV]}$ . The normalized values of  $\Gamma(T)$ ,  $\Delta(T)$  (relative to 3.5 K) appear in figure 3(c). The low effective barrier strength coupled with the strong signature of Andreev reflection show that YBCO-GaN junctions can potentially have excellent electrical properties.

In conclusion, we have demonstrated strong Andreev reflection in a YBCO-GaN junction. Theoretical modeling resulted in good agreement with experimental results. The reduced value of  $\Delta$  may be attributed to the superconducting proximity effect, which is strongly related to the phenomenon of Andreev reflection. This was achieved through the high doping of the GaN layer as well as a good contact between the YBCO and GaN layers. This demonstration of a high- $T_{\rm c}$ superconductor coupled to a wide-bandgap semiconductor can pave the way for future hybrid optoelectronic devices, working at higher temperatures around 100 K and enabling quantum optical probing of high- $T_c$  superconductivity.

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